#### Performance Evaluation of Computer Systems

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2016



















3 Performance indexes



# **Research activities in performance evaluation**

## **Teams in Grenoble**

- Polaris project : Large systems (clusters and grids)
- DataMove project : Interactive parallel systems
- Drakkar team : Networking
- Erods (Sardes) : Middleware
- Verimag : Embedded systems
- etc

## Industrial collaborations

- Orange-Lab : load injectors, performances of middlewares
- HP-Labs : cluster computing, benchmarking
- Bull : benchmarking, performances analysis
- ST-Microelectronics



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# Application context (1)

## **Complexity of computer systems**

- hierarchy : level decomposition : OS / Middleware / Application
- distribution : asynchronous resources : memory, CPU, network
- dynamicity : architecture and environment (reliability, mobility,...)
- scalability : number of components (autonomous management)

## **Typical problems**

- Minimize losses in routing policies
- Minimize active waiting in threads scheduling
- Maximize cache hits
- Optimise block sizes in parallel applications
- Maximize troughput of communication systems
- Fix time-outs, reemission periods, ...
- Fix the granularity : pages, blocks, tables, message sizes...

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# **Application context (2)**

## **Typical "hot" applications**

- Peer to peer systems : dimensionning, control
- Mobile networks : ad-hoc networking, reactivity, coherence
- Grids : resources utilization, scheduling
- etc

#### Other application domains

- production systems : production lines, logistic,...
- embedded systems
- modelling of complex systems : biology, sociology,...
- etc



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Performance indexes





# 2 Methodology

Performance indexes



## Qualitative specifications : Is the result correct ?

- property verification : formal/automatic proofs
- testing : critical dataset

## Quantitative specifications: Is the result obtained in an reasonable time ?

- performance model
- performance measurements

### Problem identification: localization of the problem

- debugging, log analysis
- performance statistical analysis

- source code / libraries / OS / architecture
- parameters of the system : dimensioning
- control algorithms : tuning

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# **Dual analysis**

## Understand the behavior of a distributed application

- identification of distributed patterns, states of the system
- 2 pattern verification
- time evaluation
- global analysis of the execution and performance synthesis
- system monitoring
- global cost evaluation for the application user

#### Understand resources utilization

- hierarchical model of resources
- evaluation of utilization at : application level; executive runtime; operating system; hardware architecture
- Iglobal cost evaluation for the resources manager

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# **Evaluation methods**



Experimentation  $\Rightarrow$  Planning experiments methodology

Performance Evaluation of Computer Systems 11 / 27

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# **Evaluation methods**





# Method

Mathematical —

Analysis (formal, numerical, approximation)

#### **Remarks :**

Hybrid methods (emulation, load injectors, synthetic programs,...) Dynamical process of evaluation Experimentation  $\Rightarrow$  Planning experiments methodology

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# **Evaluation methods**

From abstraction to physical reality			
	Model	Method	
	Mathematical>	Analysis (formal, numerical, approximation)	
	Software →>>	Simulation (discrete events)	
	Prototype>	Observation (measures)	

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# Steps for a Performance Evaluation Study (Jain)

- State the goals of the study : level of decision, investment, optimization, technical,...
- 2 Define system boundaries.
- Ist system services and possible outcomes.
- Select performance metrics.
- List system and workload parameters
- Select factors and their values.
- Select evaluation techniques.
- Select the workload.
- Obsign the experiments.
- Analyze and interpret the data.
- Present the results. Start over, if necessary.



# Aim of the course

## Objective

- Be able to analyze and predict performances of computer systems
- Be able to build a software environment that produces the performances indexes.

#### Methods

- Specification and identification of problems : modeling
- Analysis of quantitative models : formal, numerical, simulation
- Experimentation and statistical data analysis.



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**Performance indexes** 

# Organization of the course

## Performance evaluation of systems 10 cours + 10 TD/TP

http://mescal.imag.fr/membres/arnaud.legrand/teaching/2013/RICM4\_EP.php

## **Evaluation**

Experimental project



**Performance indexes** 

# Organisation

### Team



Arnaud Legrand Simulation for large scale systems analysis and control



Jean-Marc Vincent Markovian modeling of systems, simulation and dimensioning



## **References : text books**

• The Art of Computer Systems Performance Analysis : Techniques for Experimental Design, Measurement, Simulation and Modeling. Raj Jain Wiley 1991 (nouvelles versions)

Covers the content of the course, a complete book

- Performance Evaluation Jean-Yves Le Boudec EPFL electronic book http://icalwww.epfl.ch/perfeval/lectureNotes.htm Covers the statistical part of the course
- Measuring Computer Performance: A Practitioner's Guide David J. Lilja Cambridge
  University press 2000

Covers the practical part of measurement and benchmarking

 Discrete-Event System Simulation Jerry Banks, John Carson, Barry L. Nelson, David Nicol, Prentice Hall, 2004

Covers the part on simulation



# **References : journals and conferences**

- General: JACM, ACM Comp. Surv., JOR, IEEE TSE,...
- Specialized: Performance Evaluation, Operation research, MOR, ACM TOMACS, Queueing Systems, DEDS, ...
- Application: IEEE TPDS, TC, TN, TAC, Networks,...
- Theoretical: Annals of Probability, of Appl. Prob, JAP, Adv. Appl. Prob,...
- Conferences on performances: Performance, ACM-SIGMETRICS, TOOLS, MASCOT, INFORMS, ...
- Conferences on an application domain: ITC, Europar, IPDPS, Renpar, ...
- National seminars: Atelier d'évaluation de performances,...



Performance indexes



## Scientific context

Methodology





# Networking

### **Flow performance**

- latency, waiting time, response time
- loss probability
- jitter

#### **Operator performance**

- bandwidth utilisation
- achievable throughput
- loss rate

#### **Quality of service**

contract between user and provider service guarantees tradeoff between utilization and QoS

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### **Program execution**

- makespan, critical path
- speedup, efficiency
- active waiting, communication overlapping
- throughput

### System utilization

- cpu utilization, idle time
- memory occupancy
- communication throughput

### Parallel programming and scheduling

granularity of the application tradeoff between utilization and makespan

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# **Distributed applications**

## **Application**

- response time
- reactivity
- throughput (number of processed requests/unit time)
- streaming rate

#### System utilization

- service availability
- resource utilization
- communication throughput

#### System security

- reliability (error-free period)
- availability

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# **Synthesis**

## User point of view

optimize its own performance

- get the maximum amount of resources for its own purpose
- guarantee the higher quality of service

#### Resource point of view

Contract between users and resources:

- guarantee of "equity
- optimize the use of resources
- minimize costs by identifying performance bottlenecks

# Tradeoff Performance - Cost



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# Why experiments ?

### **Design of architectures, softwares**

- System debugging (!!)
- Validation of a proposition
- Qualification of a system
- Dimensioning and tuning
- Comparison of systems

Many purposes  $\Rightarrow$  different methodologies



# **Modeling fundamentals**

## **Scientific Method**

**Falsifiability** is the logical possibility that an assertion can be shown false by an observation or a physical experiment. [Popper 1930]

## Modeling comes before experimenting

## Modeling principles [J-Y LB]

- (Occam:) if two models explain some observations equally well, the simplest one is preferable
- (Dijkstra:) It is when you cannot remove a single piece that your design is complete.
- (Common Sense:) Use the adequate level of sophistication.



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# **Design of models (introduction)**

### Formulation of the question

Give explicitly the question (specify the context of experimentation)

- Identify parameters (controlled and uncontrolled)
- Identify factors (set levels)
- Specify the response of the experiment

Minimize the number of experiments for a maximum of accuracy



# Ouvrages de référence orientés évaluation de performances



Performance evaluation of computer and communication systems, Jean-Yves Le Boudec, EPFL Press 2011 Arkov Chains, Pierre Brémaud,

Springer 2001

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# Ouvrages de référence orientés évaluation de performances



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